

# **Inferring average radiative efficiency of accretion in ULXs from their XLF**

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# Radiative efficiency of accretion

$$L(\dot{M}) = \eta(\dot{M}) \times \dot{M}c^2$$

radiative efficiency of accretion

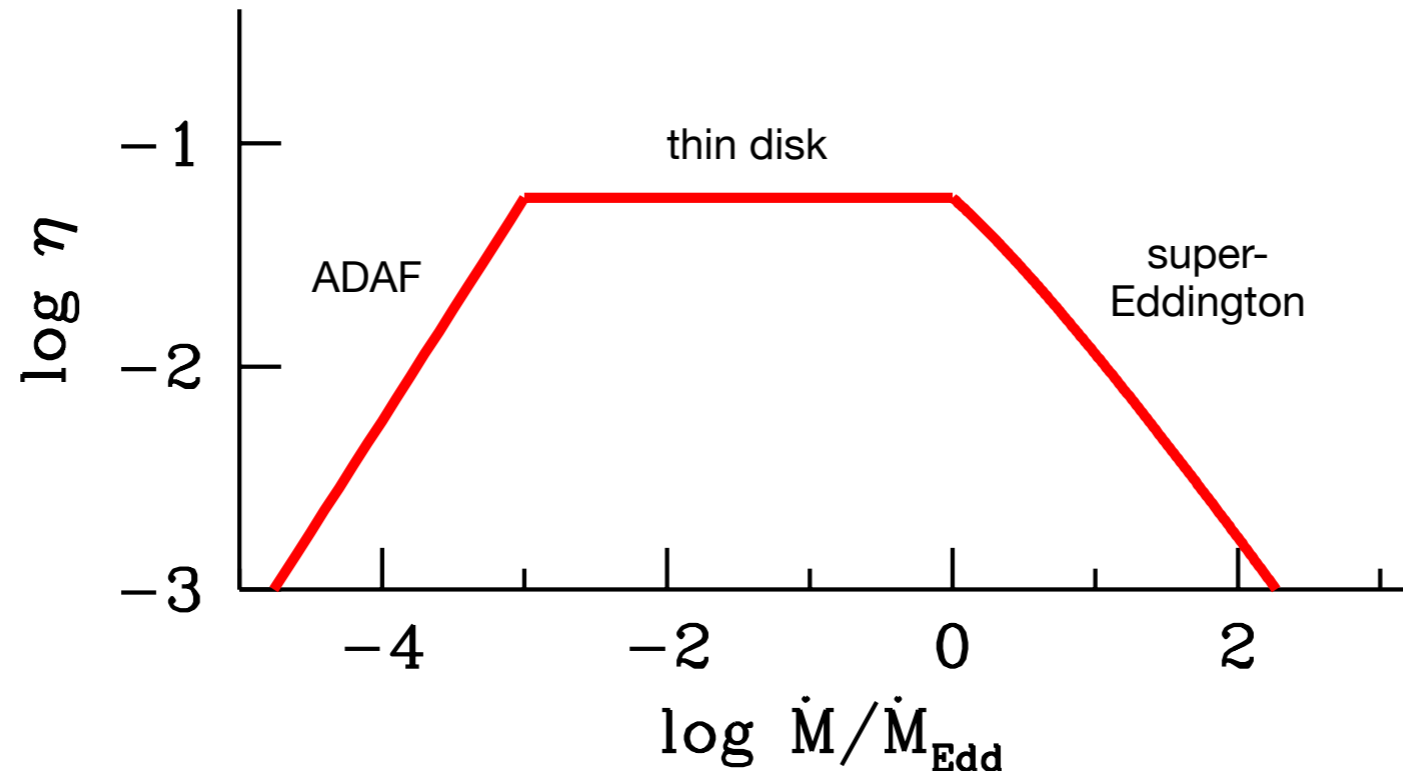
$$\eta(\dot{M}) = \frac{L(\dot{M})}{\dot{M}}$$

is difficult to measure (main difficulty is  $\dot{M}$ )

$\dot{M}$  - mass transfer rate (e.g. at the Roche lobe or Bondi radius)

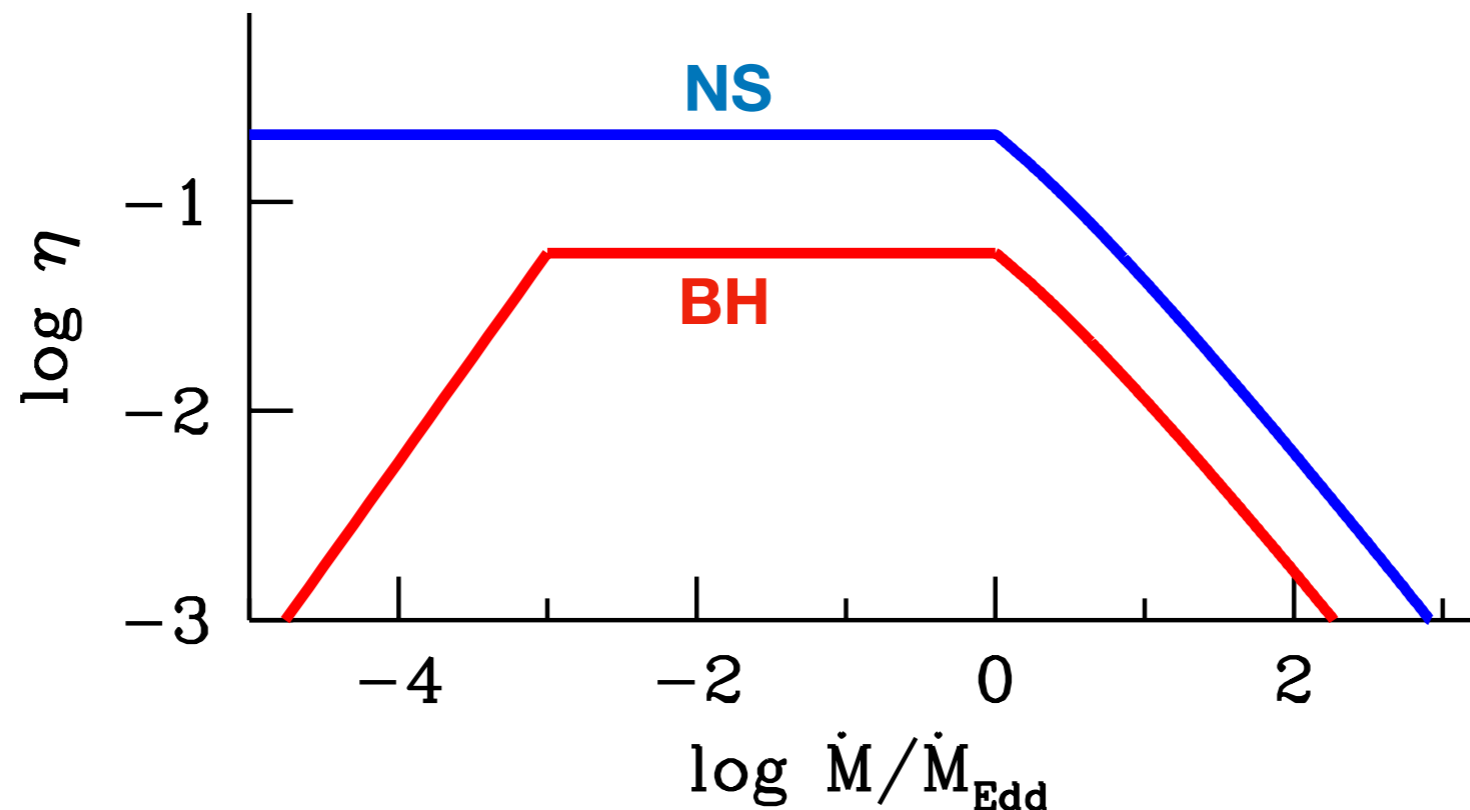
$L$  - bolometric (mostly X-ray) luminosity

# Radiative efficiency of accretion (BH)



- thin Shakura-Sunyaev disk:  $\eta \sim \text{const}$  (=0.057 for a nr BH)
- ADAF at small  $\dot{M}$ :  
(Naraya & Yi; Narayan+1998)  $\eta \sim \dot{m}$
- super-Eddington regime:  
(Shakura & Sunyaev 1973;  
Abramowicz+ 1988)  $\eta \sim \frac{\ln \dot{m}}{\dot{m}}, \quad L = L_{Edd} \times (1 + \ln \dot{m})$

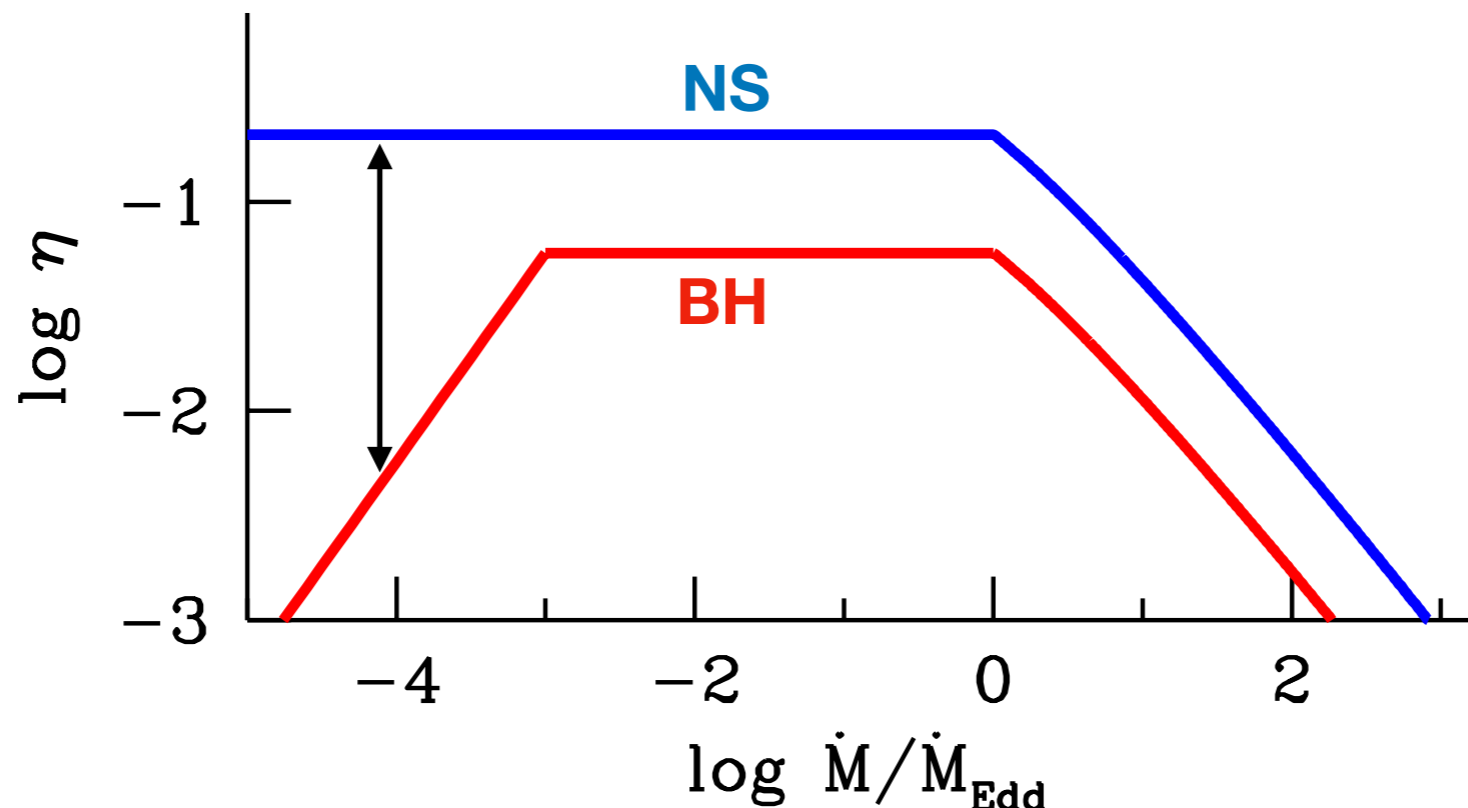
# Radiative efficiency of accretion in BH and NS



- boundary layer near NS surface  $\sim$ doubles the luminosity:  
non-rotating NS:  $\eta = 0.21$  (EOS FPS, Sibgatullin & Sunyaev 2000)
- ADAF regime still exists, but no drop of the total accretion efficiency (Yi et al., 1996)

# Radiative efficiency of accretion in BH and NS

Narayan,  
Garcia,  
McClintock  
1997



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**A method to measure the  
radiative efficiency of accretion  
in the population average sense**

# Relation between XLF and Mdot distribution

$$L = L(\dot{M})$$

$$\frac{dN}{dL} = \frac{dN}{d\dot{M}} \times \frac{d\dot{M}}{dL}$$

$$\int_L^{\infty} \frac{dN}{dL} dL = \int_L^{\infty} \frac{dN}{d\dot{M}} \times \frac{d\dot{M}}{dL} dL$$

$$\int_L^{\infty} \frac{dN}{dL} dL = \int_{\dot{M}(L)}^{\infty} \frac{dN}{d\dot{M}} d\dot{M}$$

$$N(> L) = N(> \dot{M}(L))$$

# Population averaged accretion efficiency

$$N(> L) = N(> \dot{M}(L))$$

XLF of X-ray binaries  
known!

distribution of binaries over  
mass-transfer rate:

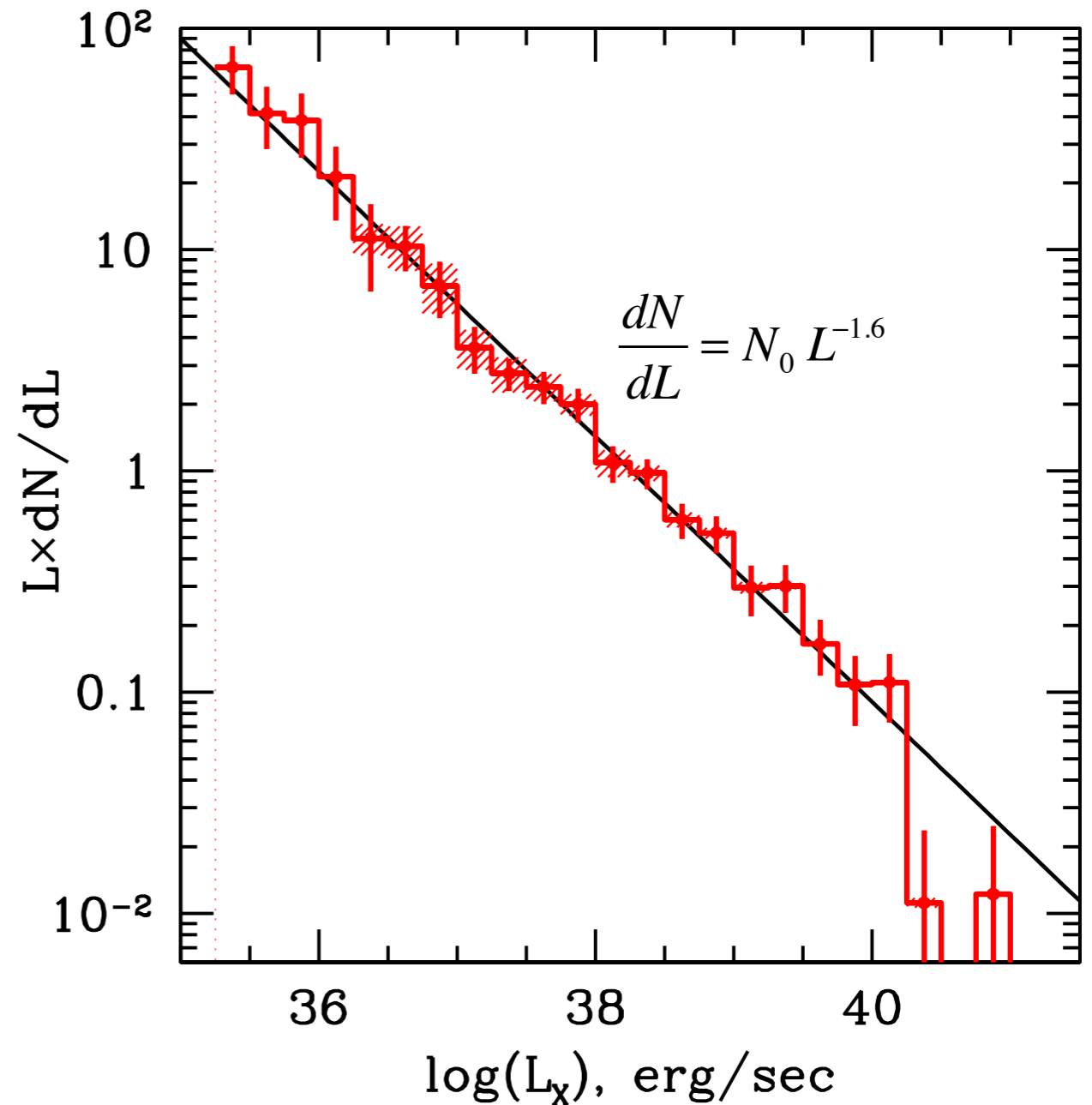
- from observations (difficult!)
- from binary population synthesis calculation
- inferred from some other considerations



# X-ray luminosity function of HMXBs

a power law with a roll-over or a cut-off at  $\log(L_x) \sim 40$

Grimm, MG, Sunyaev, 2003  
Swartz et al., 2004, 2011  
Mineo, MG, Sunyaev, 2012



# Mdot distribution

at  $\log(L_x) \sim 35 \dots 38$  (thin disk case) one should expect

$$L = \eta_0 \dot{M} c^2$$

$$\frac{dN}{d\dot{M}} = \eta_0 c^2 \frac{dN}{dL} \Rightarrow \frac{dN}{d\dot{M}} = N_0 (\eta_0 c^2)^{-0.6} \dot{M}^{-1.6}$$

assuming that  $\frac{dN}{d\dot{M}} = N_0 (\eta_0 c^2)^{-0.6} \dot{M}^{-1.6}$  in the entire  $\dot{M}$  range of interest

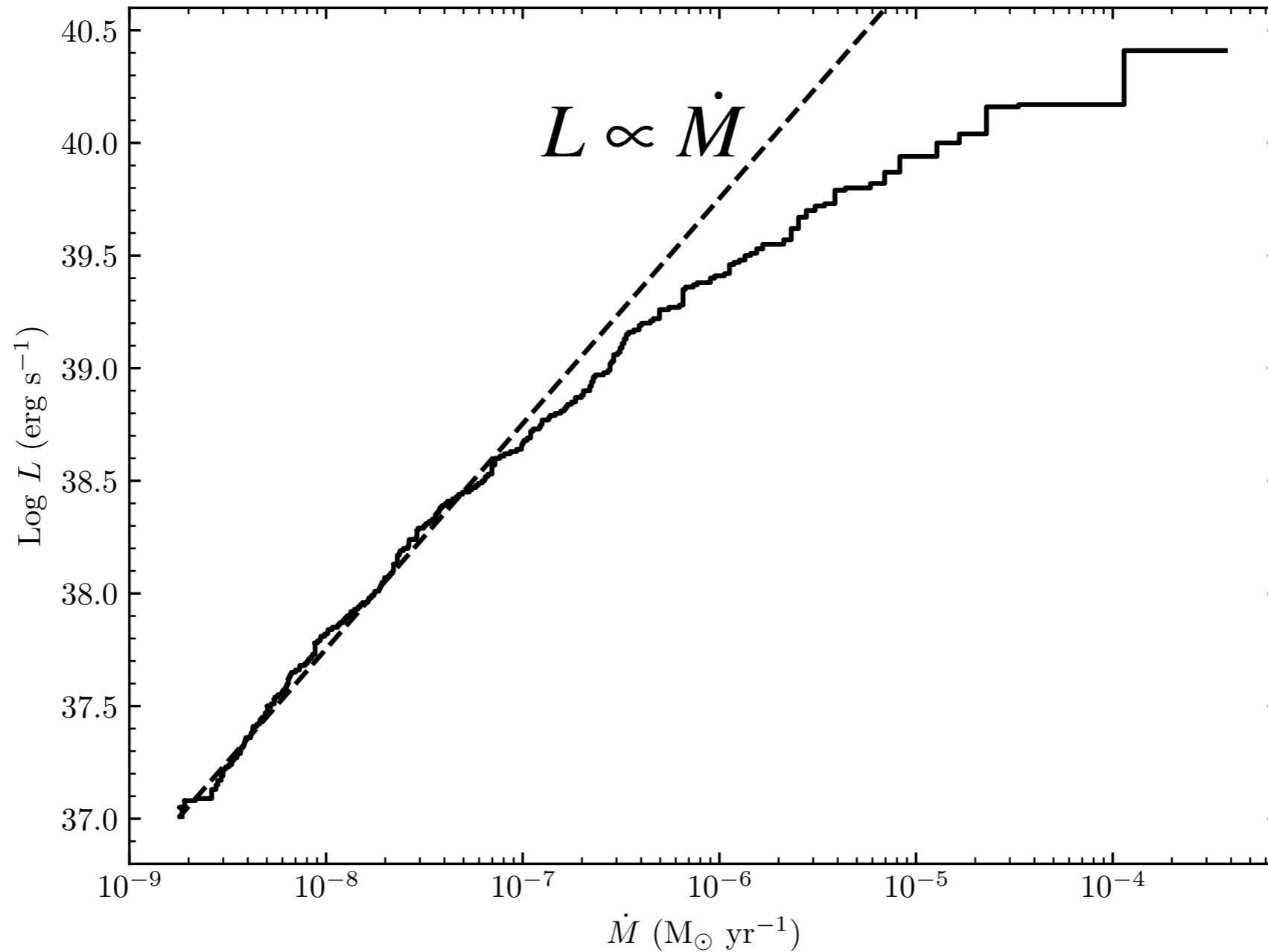
we obtain:

$$\dot{M}(L) = \frac{1}{\eta_0 c^2} \left[ \frac{0.6 N(>L)}{N_0} \right]^{-\frac{1}{0.6}} \quad \text{and} \quad \eta = \eta_0 \frac{L N_0^{-\frac{1}{0.6}}}{[0.6 N(>L)]^{-\frac{1}{0.6}}}$$

where  $N(>L)$  is the observed XLF of HMXBs

This formula is valid as long as  $\frac{dN}{d\dot{M}} \propto \dot{M}^{-1.6}$  extends to sufficiently high  $\dot{M}$

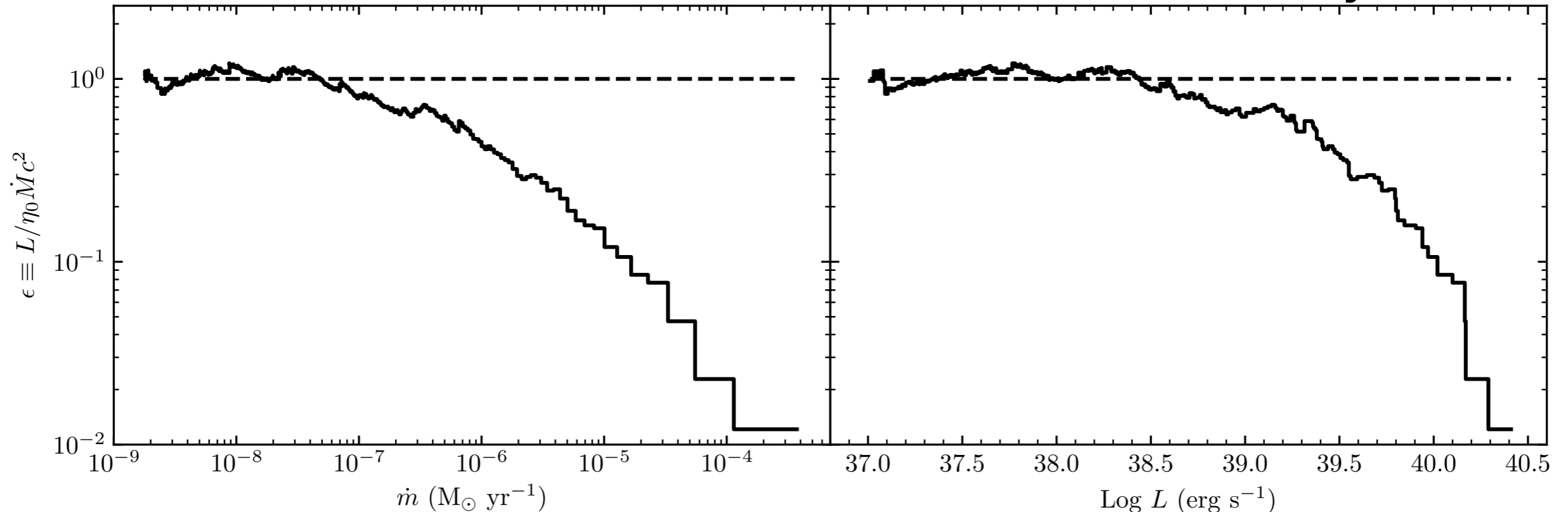
# Average Mdot-L<sub>x</sub> relation for HMXBs



# Average radiative efficiency of HMXBs

vs. Mdot

vs. luminosity



- nearly constant at  $\log(L_X) \leq 38.5$
- starts to decline near  $L_{Edd}$  for a neutron star
- drops down by a factor of  $\sim 10$  in the ULX regime  
brightest ULXs must be fed at  $\sim 10^{-5} M_{\text{sun}}/\text{yr}$

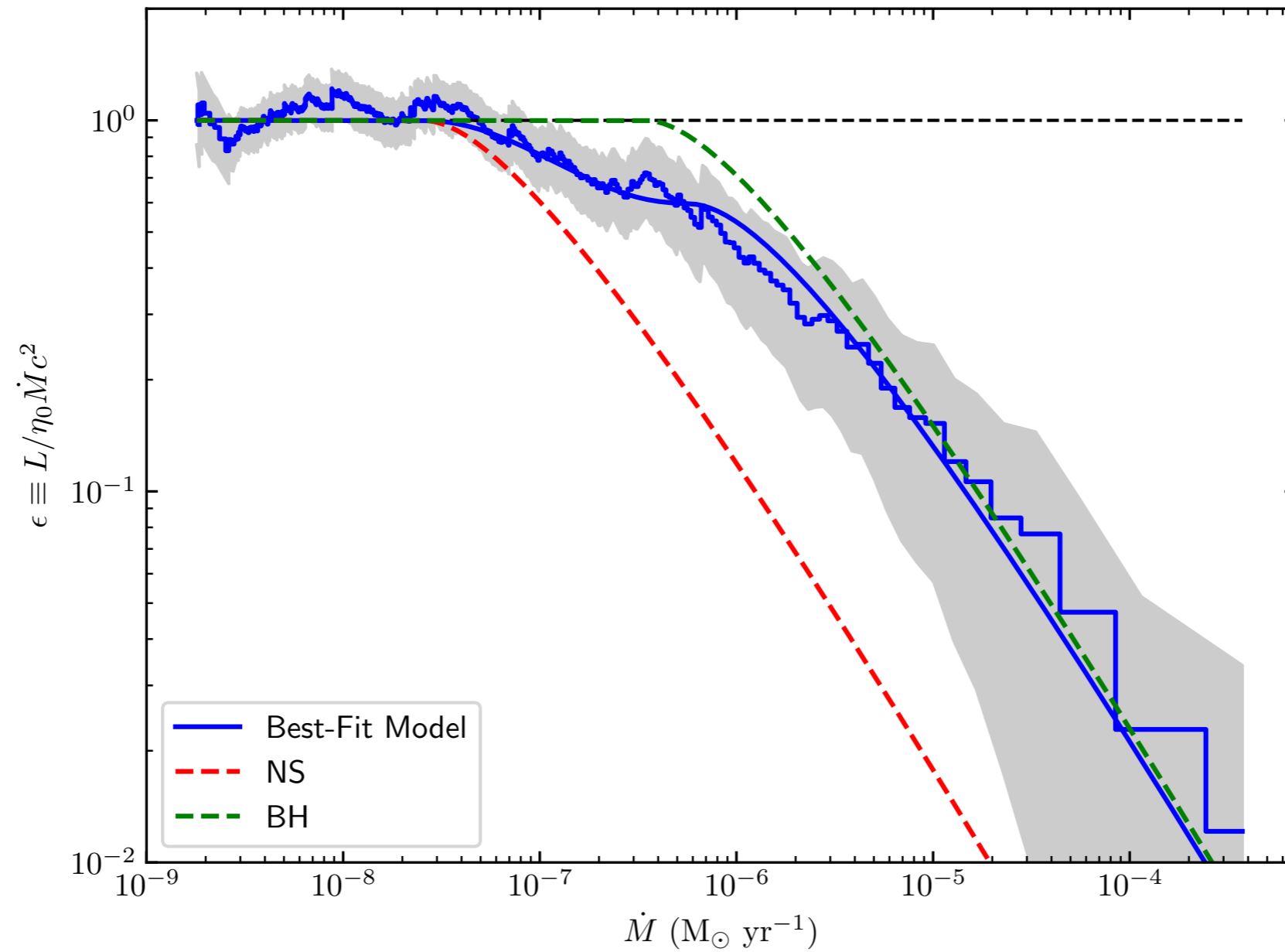
# Fit with a $L_X = L_{Edd} (1 + \ln \dot{m})$ model

- one population model does not work
- a model of two populations with different  $L_{Edd}$  good fit
- parameters of the two populations:

| population  | mass                            | fraction        |
|-------------|---------------------------------|-----------------|
| light (=NS) | $1.0^{+0.62}_{-0.36} M_{\odot}$ | $0.26 \pm 0.10$ |
| heavy (=BH) | $13.5^{+3.5}_{-2.3} M_{\odot}$  | $0.74 \pm 0.10$ |

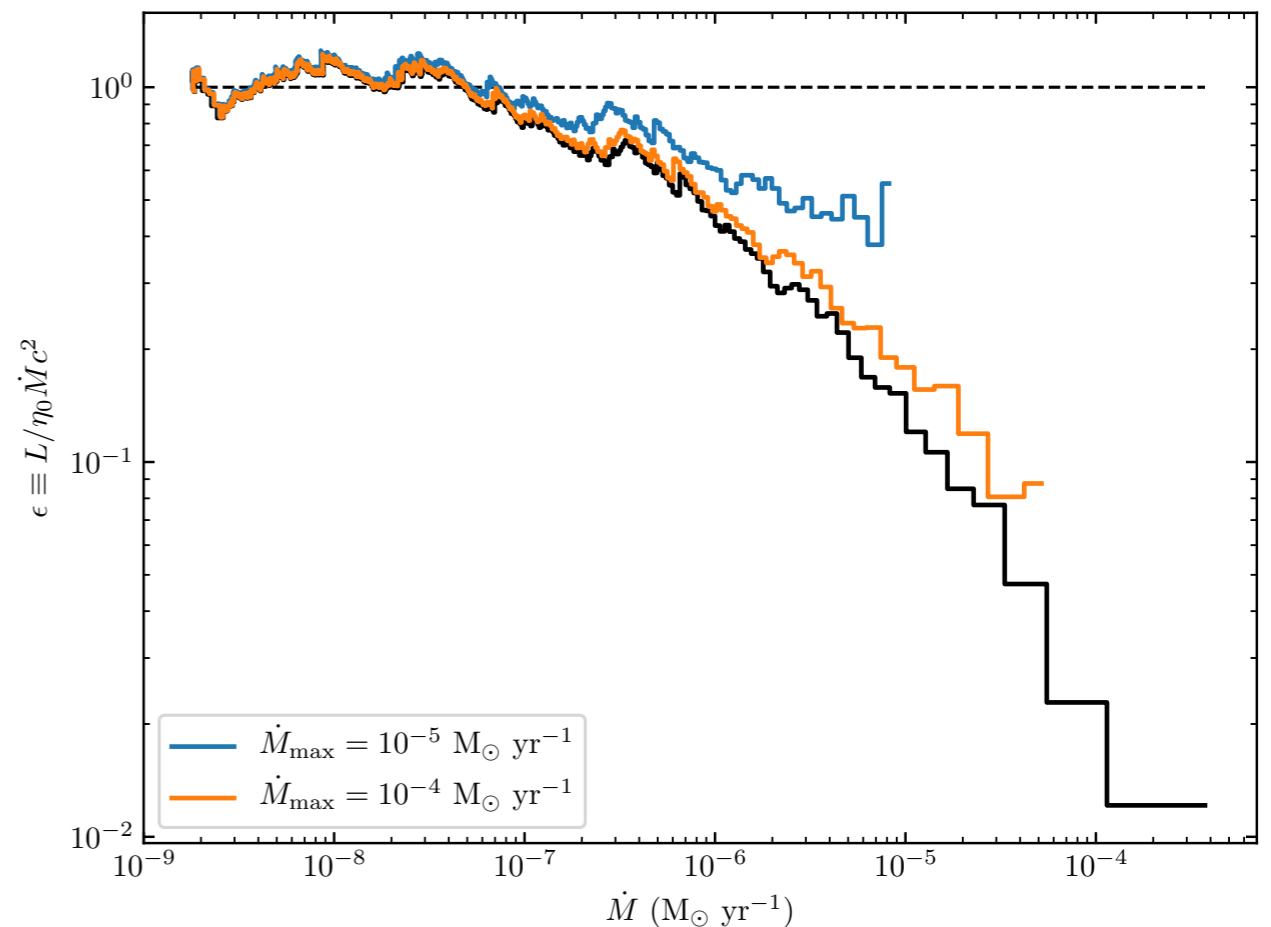
- model require large fraction of the BH population

# Best-fit two population model



# Impact of a cut-off in the $\dot{M}$ distribution

- it was assumed that  $\frac{dN}{d\dot{M}} \propto \dot{M}^{-1.6}$  continues to  $\dot{M} > 10^{-4} M_{\odot} / yr$
- if the  $\dot{M}$  - distribution significantly steepens at  $\dot{M} \sim 10^{-5} M_{\odot} / yr$  average radiative efficiency in ULXs must be high
- conversely,  $\dot{M}$ -distribution can not be significantly steeper than the  $\dot{M}^{-1.6}$  law much below  $\dot{M} \sim 10^{-6} M_{\odot} / yr$



# Summary

- population average radiative efficiency of ULXs:
  - nearly constant at  $\log(L_X) \leq 38.5$
  - starts to decline near  $L_{Edd}$  for a neutron star
  - drops down by a factor of  $\sim 10$  in the ULX regime  
brightest ULXs must be fed at  $\sim 10^{-5}$  Msun/yr and lose about  $\sim 90\%$  of the material in outflows
  - shape is well described by the  $\propto (1 + \ln \dot{m})$  law
- can be well approximated with a two population model with masses of populations close to NS and BH masses
- the model does not anticipate existence of ULX pulsars which may not have much impact due to their relatively small numbers



**Thank you!**