A Typical Sherpa Session

(The boiled-down version.)

The user:

- reads in data (and sets filters, etc.);
- builds model expressions;
- chooses a statistic;
- fits the model expressions to the data, one at a time;
- compares the results of the fits in order to select a best-fit model; and
- estimates the errors for the best-fit model parameters.

Choosing a Statistic

(So many choices, so little guidance.)

A key feature of Sherpa is its large array of statistics appropriate for analyzing Poisson-distributed (i.e. counts) data.

- Statistics based on χ^2 :
 - CHI GEHRELS
 - CHI DVAR
 - CHI MVAR
 - CHI PARENT
 - CHI PRIMINI
- \bullet Statistics based on the Poisson likelihood \mathcal{L} :
 - -CASH
 - BAYES

If the data are not Poisson-distributed (e.g. fluxes), then alternatives include:

- least-squares fitting: setting all variances to one; or
- providing errors in an input file.

χ^2 -Based Statistics

The χ^2 statistic is

$$\chi^2 \equiv \sum_i \frac{(D_i - M_i)^2}{\sigma_i^2},$$

where

- D_i represents the observed datum in bin i;
- M_i represents the predicted model counts in bin i; and
- σ_i^2 represents the variance of the sampling distribution for D_i .

$$\chi^2$$
 Statistic σ_i^2

GEHRELS
$$[1 + \sqrt{D_i + 0.75}]^2$$

$${ t DVAR}$$

$$exttt{MVAR} \qquad \qquad M_i$$

PARENT
$$\frac{\sum_{i=1}^{N} D_i}{N}$$

PRIMINI
$$M_i$$
 from previous best-fit

Likelihood-Based Statistics

The CASH statistic is

$$C \equiv 2\sum_{i} [M_i - D_i \log M_i] \propto -2 \log \mathcal{L},$$

where

- D_i represents the observed datum in bin i;
- M_i represents the predicted model counts in bin i; and
- $\mathcal{L} = \prod_i \frac{M_i^{D_i}}{D_i!} \exp(-M_i).$

Statistics: Caveats

(Potholes on the road to publication.)

Things to remember when using χ^2 :

- χ^2 is an approximation of $\log \mathcal{L}$ in the Gaussian (high-counts) limit. So...
- All estimations of variance (except GEHRELS) assume a Gaussian sampling distribution, not Poisson. Hence the number of counts in each bin should be ≥ 5 .
- CHI GEHRELS works with low-count data, but does not generally follow the χ^2 distribution: best fits are often "too good."
- And χ^2 is a biased estimator.

Things to remember when using CASH or BAYES:

- In the limit of high counts, $\Delta C \sim \Delta \chi^2$.
- Likelihood estimators are unbiased. But...
- Background subtraction is *not* allowed.
- There is no "goodness-of-fit" measure.
- And negative model amplitudes are *not* allowed.

Optimization in Sherpa

Optimization is the action of minimizing χ^2 or $-\log \mathcal{L}$ by varying the thawed parameters of the model. The user may choose between several optimization methods in Sherpa, including ones which:

- Find the local minimum.
 - POWELL
 - SIMPLEX
 - LEVENBERG-MARQUARDT

These algorithms are not computationally expensive, but they are also not appropriate for finding the global minimum of a complex statistical surface when starting from a random point.

- Attempt to find the global minimum.
 - GRID and GRID-POWELL
 - MONTE and MONTE-POWELL
 - SIMULATED ANNEALING

These are computationally intensive algorithms which are useful for searching complex statistical surfaces, starting from a random point.

Main SHERPA Components

- Data Input/Output.
- Visualization through ChIPS and ds9
- Model library and model language.
- Statistics and Error Analysis.
- Optimization Methods.

MODELS

• Three main type of models:

Source

Background

Instrument

- Model library consists of several models (plus XSPEC v.11) which can be used to define a source or background model.
- There are three type of instrument models:

RSP

PsfFromTCD

PsfFromFile

- Instrument models are convolved with Source and Background models before the model predicted data is compared with the observed data.
- Instrument and Background models are NOT required. Source models have to be defined for fitting.

Data Entry

- During a *Sherpa* session, the user may read in files containing:
 - source data
 - background data
 - errors on the source and/or background data
 - filters
 - statistical weights

These data may be integer, float, or double precision and may be of arbitrary dimensionality.

- Currently supported file types include:
 - ASCII
 - FITS binary table
 - FITS image
 - PHA types I & II
 - IRAF imh
 - ROSAT qpoe

For all types except ASCII, data entry is accomplished through the Data Model interface, so that, *e.g.*, one can use the Data Model filtering syntax within *Sherpa* data entry commands.

Instrument Models

- Instrument models describe the mapping from photon space (where source and background models are evaluated) to counts space (where fit statistics are computed) for a particular detector.
 - ⇒ The instrument model class, by hiding detectordependent details, allows Sherpa to be a missionindependent fitting application.
- Currently *Sherpa* offers three instrument model types:
 - RSP, in which the evaluated one-dimensional model is multiplied by an ancillary response (*i.e.* effective area) and then folded through a response matrix;
 - PSFFromTCD, in which the evaluated one- or two-dimensional model is convolved with an analytic kernel (e.g. Gaussian) defined in CIAO's TCD library;
 - and PSFFromFile, in which the evaluated two-dimensional model is convolved with a numeric kernel.

Building Model Expressions

- In *Sherpa*, one can build model expressions that represent the
 - source
 - background
 - instrument

for each dataset.

- \Rightarrow Note, however, background and instrument model expressions are *not* required to carry out fits.
- Currently, nearly 40 one- and two-dimensional *Sherpa* models and 90 one-dimensional *XSPEC v. 11* models are available for building model expressions.

Building Model Expressions

- Model parameters can be *linked* to other parameters.
- Example:
 - A particular atomic line is observed by detectors with different resolutions. One can model this line with two Gaussian functions whose centroids (but not amplitudes or widths) are linked:

```
sherpa> source 1 = gauss1d[g1]
sherpa> source 2 = gauss1d[g2]
sherpa> g1.pos => g2.pos
```

- Model parameters can also be linked to other models.
- Example:
 - One can model emission from an accretion disk using a blackbody function whose temperature is a function of radius:

```
sherpa> Temperature = POLY
sherpa> BB.kT => Temperature
```

Building Model Expressions

- A model can be *nested* within another model.
- Example:
 - Transform an input dataspace to log-space, and evaluate a blackbody in that space:

```
sherpa> logenergy = shlog
sherpa> source = bb{logenergy}
```

- Different models can be defined along each axis of a multi-dimensional dataset.
- Example:
 - Model two-dimensional data that have spectral information along one axis and spatial information (e.g. radius) along the other:

```
sherpa> data image.fits
sherpa> lorentz[Spatial]
sherpa> pow[Spec]
sherpa> source = Spatial{x1}*Spec{x2}
```